



The Connection Between Neutrino CP Violation and Leptogenesis

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NASA Hubble Photo

A major motivation to look for ~~CP~~ in neutrino oscillation:
 Its observation would make **leptogenesis** more plausible.

Leptogenesis

Explains the baryon-antibaryon asymmetry of the universe by CP-violating heavy neutrino decays.

Heavy ($m_N > 10^9$ GeV)
Majorana neutrino

SM lepton

SM Higgs

$$\Gamma(N \rightarrow \ell^- + H^+) \neq \Gamma(N \rightarrow \ell^+ + H^-)$$

The diagram illustrates the decay of a heavy Majorana neutrino (N) into a Standard Model (SM) lepton (ℓ) and a Standard Model Higgs boson (H). The decay is shown to be CP-violating, as the decay rate for $N \rightarrow \ell^- + H^+$ is not equal to the decay rate for $N \rightarrow \ell^+ + H^-$. The heavy neutrino is labeled as 'Heavy ($m_N > 10^9$ GeV) Majorana neutrino'. The decay products are labeled as 'SM lepton' and 'SM Higgs'.

This ~~CP~~ creates a **lepton-antilepton** asymmetry.

The SM Sphaleron process converts part of this asymmetry into the observed **baryon-antibaryon** asymmetry.

Leptogenesis is an outgrowth of the **See-Saw** theory of why neutrinos are so light.

The straightforward (type-I) See-Saw theory adds to the SM Lagrangian just —

$$\mathcal{L}_{\text{new}} = -\frac{1}{2} \sum_i m_{N_i} N_i^2 + \sum_{\substack{\alpha=e,\mu,\tau \\ i=1,2,3}} y_{\alpha i} \left[\bar{\nu}_\alpha \overline{H^0} - \bar{\ell}_\alpha H^- \right] N_i + h.c.$$

Majorana masses

SM lepton doublet

SM Higgs doublet

Yukawa coupling matrix

~~CP~~ in N decays comes from ~~CP~~ phases in y .

Number of leptonic parameters in the See-Saw picture: **21**

Number of these parameters that can be measured
without producing the heavy neutrinos N : **12**

Since **21 > 12**, laboratory measurements today
cannot pin down what happened in the early universe.

Can there be ~~CP~~ in ν oscillation but no leptogenesis? Yes.

Can there be leptogenesis but no ~~CP~~ in ν oscillation? Yes.

Is either of these possibilities likely? **NO!**

An Argument

(BK, arXiv:1012.4469)

The See-Saw Relation

Leptonic mixing matrix } Heavy N mass eigenvalues

$$UM_{\nu}U^T = -v^2 \left(y M_N^{-1} y^T \right)$$

Light ν mass eigenvalues } The Higgs vev, a real number

$$\left(\underbrace{UM_{\nu}U^T}_{\text{Outputs}} = -v^2 \underbrace{\left(y M_N^{-1} y^T \right)}_{\text{Inputs, in } \mathcal{L}} \right)$$

Through U , the phases in \mathbf{y} lead to \cancel{CP} in light neutrino oscillation.

$$\begin{aligned}
 P(\overset{(-)}{\nu}_\alpha \rightarrow \overset{(-)}{\nu}_\beta) &= \\
 \text{e, } \mu, \text{ or } \tau & \begin{array}{c} \uparrow \quad \uparrow \\ \hline \end{array} \\
 &= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right) \\
 & \quad \overset{\text{Distance}}{\downarrow} \quad \uparrow \\
 & \quad \overset{\text{Neutrino (Mass)}^2 \text{ splitting}}{\uparrow} \quad \overset{\text{Energy}}{\uparrow} \\
 & \quad \overset{(+)}{\underset{(-)}{2}} \sum_{i>j} \Im(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin\left(\Delta m_{ij}^2 \frac{L}{2E}\right)
 \end{aligned}$$

Generically, leptogenesis and light-neutrino \cancel{CP} imply each other.

If all N_i masses $> 10^{12}$ GeV, then the phases that drive leptogenesis are independent of those in U .

However, supersymmetry suggests that the lightest N_i must have mass $\sim 10^9$ GeV.

Then \cancel{CP} phases in U , which produce \cancel{CP} in ν oscillation, and influence the rate for neutrinoless double beta decay, lead also to a baryon-antibaryon asymmetry.

(Casas, Ibarra; Kohri, Moroi, Yotsuyanagi; Abada, Davidson, Ibarra, Josse-Michaux, Losada, Nardi, Nir, Racker, Riotto, Roulet; Pascoli, Petcov, Riotto, Rodejohann)

Summary

Generically, leptogenesis and light-neutrino \mathcal{CP} do imply each other.

